A classification of Hénon maps in the presence of strange attractors

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In my talk I shall present my work with Sonja Štimac from [1]-[2] on Hénon maps with strange attractors (Wang-Young parameters [6]-[7]). First I shall explain a construction, inspired by a work of Crovisier and Pujals on mildly dissipative diffeomorphisms of the plane [3]-[5], of conjugacy of these maps to the shift homeomorphisms on inverse limits of dendrites with dense set of branch points, and a characterization of orbits of critical points in terms of these inverse limits. Then I will explain how this leads to a classification of conjugacy classes of such maps in terms of a single sequence of 0s and 1s.

References

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